## MA.5.AR.1.2

Overarching Standard: *MA.5.AR.1: Solve problems involving the four operations with whole numbers and fractions.* 

Benchmark of Focus

MA.5.AR.1.2: Solve real-world problems involving the addition, subtraction or multiplication of fractions, including mixed numbers and fractions greater than 1.

*Examples:* Shanice had a sleepover, and her mom is making French toast in the morning. If her mom had  $2\frac{1}{4}$  loaves of bread and used  $1\frac{1}{2}$  loaves for the French toast, how much bread does she have left?

**Benchmark Clarifications** 

*Clarification 1:* Instruction includes the use of visual models and equations to represent the problem.

## Related Benchmark/Horizontal Alignment

- MA.5.FR.2.1
- MA.5.FR.2.2
- MA.5.M.1.1
- MA.5.GR.2.1
- MA.5.DP.1.1

Vertical Alignment	
Previous Benchmarks MA.4.AR.1.2	Next Benchmarks
MA.4.AR.1.3	MA.6.NSO.2.3

Purpose and Instructional Strategies

The purpose of this benchmark is to continue the work from Grade 4 (MA.4.AR.1.2/1.3) where students began solving real-world with fractions, and prepares them for Grade 6 (MA.6.NSO.2.3) where they will solve real-world fraction problems using all four operations with fractions. (MTR.7.1).

- Students need to develop an understanding that when adding or subtracting fractions, the fractions must refer to the same whole.
- During instruction, teachers should provide opportunities for students to practice solving problems using models or drawings to add, subtract or multiply with fractions. Begin with students modeling with whole numbers, have them explain how they used the modelor drawing to arrive at the solution, then scaffold using the same methodology using fraction models.
- Models to consider when solving fraction problems should include, but are not limited to,area models (rectangles), linear models (fraction strips/bars and number lines) and set models (counters) (MTR.2.1).
- Please note that it is not expected for students to always find least common multiples or make fractions greater than 1 into mixed numbers, but it is expected that students know and understand equivalent fractions, including naming fractions greater than 1 as mixed numbers to add, subtract or multiply.

• It is important that teachers have students rename the fractions with a common denominator when solving addition and subtraction fraction problems in lieu of the "butterfly" method (or other shortcut/mnemonic) to ensure students build a complete conceptual understanding of what makes solving addition and subtraction of fractionsproblems true.

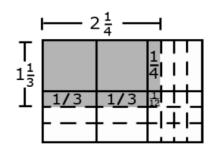
Common Misconceptions or Errors

- When solving real-world problems, students can often confuse contexts that require subtraction and multiplication of fractions. For example, "Mark has <sup>3</sup>/<sub>4</sub> yards of rope and he gives half of the rope to a friend. How much rope does Mark have left?" expects students to find <sup>1</sup>/<sub>2</sub> of <sup>3</sup>/<sub>4</sub>, or multiply <sup>1</sup>/<sub>2</sub> x <sup>3</sup>/<sub>4</sub> to find the product that represents how much is given to the friend. On the other hand, "Mark has <sup>3</sup>/<sub>4</sub> yards of rope and gives <sup>1</sup>/<sub>2</sub> yard of rope to a friend. How much rope does Mark have left?" expects students. How much rope does Mark have left?" expects students to take <sup>1</sup>/<sub>2</sub> yard of rope to a friend. How much rope does Mark have left?" expects students to take <sup>1</sup>/<sub>2</sub> yard from <sup>3</sup>/<sub>4</sub> yard, or subtract <sup>3</sup>/<sub>4</sub> <sup>1</sup>/<sub>2</sub> to find the difference. Encourage students to lookfor the units in the problem (e.g., <sup>1</sup>/<sub>2</sub> yard versus <sup>1</sup>/<sub>2</sub> of the whole rope) to determine the appropriate operation.
- Students may believe that multiplication always results in a larger number. Using models when multiplying with fractions will enable students to generalize about multiplication algorithms that are based on conceptual understanding (MTR.5.1).
- Students can have difficulty with word problems when determining which operation to use, and the stress of working with fractions makes this happen more often.
  - For example, "Mark has  $\frac{3}{4}$  yards of rope and he gives a third of the rope to a friend. How much rope does Mark have left?" expects students to first find  $\frac{1}{3}$  of  $\frac{3}{4}$  or multiply  $\frac{1}{3} \times \frac{3}{4}$ , and then to find the difference to find how much Mark has left. On the other hand, "Mark has  $\frac{3}{4}$  yards of rope and gives  $\frac{1}{3}$  yard of rope to a friend. How much rope does Mark have left?" only requires finding the difference of  $\frac{3}{4} \frac{1}{3}$ .

Questions to ask students:

- Ask students how they knew to add or subtract the fractions based on the actions in the word problem.
- Sample answer that indicates understanding: Students may describe actions that involve the combination of amounts or distances OR the act of determining the difference between two fractions.
- In this problem situation, how did you know to multiply?
- Sample answer that indicates understanding: In the problem, I know the number of groups and the number in each group so I am looking for the product. This makes it a multiplication problem.
- Why did you draw this type of model when solving this problem?
- Sample answer that indicates understanding: If I have 3 pieces of ribbon and each piece is 2 ½ inches long, I need to multiply to show 3 groups of 2 ½ inches. My number line model shows the 3 groups of 2 ½ inches.
- Jaden and Dariel are making a poster for a class assignment. The dimensions of the poster need to be  $1\frac{1}{3}$  feet by  $2\frac{1}{4}$  feet. What will be the total area for the poster?

• Sample answer that indicates understanding: A student draws the following to show the array made by multiplying the two factors. The student adds all the partial products in the model for a total of 3 square feet.



Instructional Tasks Instructional Task 1

Rachel wants to bake her two favorite brownie recipes. One recipe needs  $1\frac{1}{2}$  cups of flour and the other recipe needs  $\frac{3}{4}$  cups of flour. How much flour does Rachel need to bake her two favorite brownie recipes?

## Instructional Task 2

Shawn finished a 100 meter race in  $\frac{3}{8}$  of one minute. The winner of the race finished in  $\frac{1}{3}$  of Shawn's time. How long did it take for the winner of the race to finish?

Instructional Items Instructional Item 1

Monica has  $2\frac{3}{4}$  cups of berries. She uses  $\frac{5}{8}$  cups of berries to make a smoothie. She then uses  $\frac{1}{2}$  sup for a fruit salad. After she makes her smoothie and fruit salad, how much of the berries will Monica have left?

Achievement Level Descriptors:

Benchmark	Context	Assessment Limits
MA.5.AR.1.2 Solve real-world problems involving the addition, subtraction or multiplication of fractions, including mixed numbers and fractions greater than 1. Example: Shanice had a sleepover and her mom is making French toast in the morning. If her mom had $2\frac{1}{4}$ , loaves of bread and used $1\frac{1}{2}$ , loaves for the French toast, how much bread does she have left?	Real-world	Items requiring addition or subtraction must include denominators using unlike whole numbers. Items requiring multiplication must include denominators using whole numbers up to 20.

Clarification 1: Instructio visual models and equa problem.				
ALD 2	ALD 3	ALD 4		ALD 5
Solves real-world	Solves real-world	Solves real-world		Identifies an error and
problems involving	problems involving	problems involving	the	solves multi-step, real-
addition and	addition and	addition, subtraction	n, or	world problems
subtraction of fractions	subtraction or	multiplication of		involving the addition,
with unlike	multiplication of	fractions, including		subtraction, or
denominators, using	fractions with unlike	mixed numbers and	l	multiplication of
models and various	denominators and	fractions greater tha	an	fractions, including
strategies.	those greater than one.	one.		mixed numbers and
				fractions greater than
				one.

Additional Resources: CPALMS Resources

Subtracting Fractions Word Problems

Resources/Tasks to Support Your Child at Home: <u>Multiply a Fraction by a Fraction</u>

Multiply Mixed Numbers by Mixed Numbers

Find various recipes that contain fractions and mixed number measurements. Pose addition and subtraction types of questions using the recipes.

For example: How much more sugar than flour? How much butter and milk combined? What is the total of all the ingredients in the recipe?